

1. Evaluate the following.

(a) (2 points) $\frac{d}{dx} (\ln(\sin(x)))$

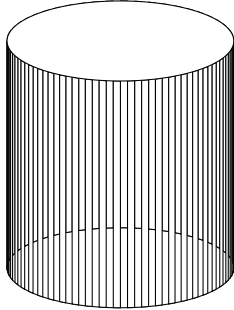
(b) (2 points) $\frac{d}{dx} (\log_7(x))$

(c) (2 points) $\frac{d}{dx} (\tan^{-1}(x^2 + 1))$

(d) (2 points) $\frac{d}{dx} (3^x)$

(e) (2 points) $\frac{d}{dx} (\cos^{-1}(\frac{1}{x}))$

2. (12 points) A solid cylinder is being heated and is growing slightly. Currently, its radius is $r = 5$ cm and its height is $h = 10$ cm. If, at this time, its radius is growing at the rate of 0.2 cm/min and its height is growing at the rate 0.1 cm/min, then at what rate is its volume increasing? Make sure you give your answer with the right units.



3. Evaluate the following limits:

(a) (5 points) $\lim_{x \rightarrow 0} \frac{1 - \cos(x)}{x^2}$

(b) (5 points) $\lim_{x \rightarrow \infty} x^{-1} \ln(x)$

4. Let $f(x) = \sqrt{4+x}$.

(a) (5 points) Find the linearization L of f at $a = 0$.

(b) (5 points) Use L to give an approximation to $\sqrt{4.1}$.

5. (12 points) Find the absolute minimum and absolute maximum of $f(x) = x^{2/3}$ on the interval $[-8, 27]$. Justify your answer. Make sure you specify where the absolute maximum and absolute minimum occur.

6. Let $f(x) = x^2 + 4x + 1$.

(a) (5 points) Does the Mean Value Theorem apply to f on the interval $[0, 2]$? Explain why or why not.

(b) (5 points) What is the average rate of change of f on $[0, 2]$?

(c) (5 points) Find c in $(0, 2)$ so that $f'(c)$ equals the average rate of change you found in part (b).

7. Let $f(x) = 12x - x^3$ on $(-3, \infty)$.

(a) (4 points) Find the coordinates of any critical points of f .

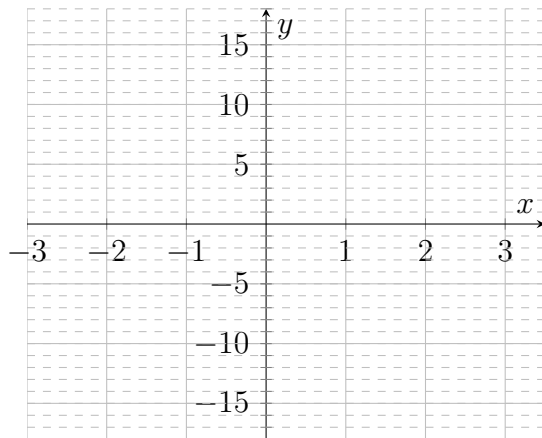
(b) (2 points) Find the intervals where f is increasing and those where f is decreasing.

(c) (2 points) Find the intervals where the graph $y = f(x)$ is concave up and those where it is concave down.

(d) (4 points) Find the inflection points of f .

(e) (4 points) Identify all of the local extrema and where they occur. Clearly mark each as a local maximum or local minimum.

(f) (4 points) Sketch the graph of $y = f(x)$ using the information from (a)-(d).



8. (11 points) A farm building has a straight wall 160 feet long. Farmer Brown wants to use 160 feet of fencing to create a rectangular fenced-in pen against the wall for Daisy Mae and her three piglets—Petunia, Porkchop, and Slim. The pen will use part of the wall as one of its sides but the other three sides of the pen will have to be created using the fencing as shown below. What are the dimensions of the pen that will give the largest area? [Drawing is not to scale.]

